

7. (a) Consider the causal linear shift-invariant filter with system function 7

$$H(z) = \frac{(1 + 0.875z^{-1})}{(1 + 0.2z^{-1} + 0.9z^{-2})(1 - 0.7z^{-1})}$$

Draw a signal flow graph for the system using direct form II.

- (b) Show that for bilinear transformation

$$S = \frac{2}{T} \left( \frac{1 - z^{-1}}{1 + z^{-1}} \right) \text{ where } T \text{ in sampling duration.} \quad 7$$

8. (a) Design a filter with 7

$$H_d(e^{-j\omega}) = \begin{cases} e^{-j3\omega}, & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0, & \frac{\pi}{4} \leq |\omega| \leq \pi \end{cases}$$

using a Hamming window with  $M=7$

- (b) Derive order formula for cheby shev filter. Assume required parameters. 7

9. (a) Determine the IDFT of  $x(u) = \{3, (2+j), 1, (2-j)\}$  7

- (b) consider the dinerete time sequence  $x[n] = \cos\left(\frac{n\pi}{8}\right)$

Find two different continuous time signal, that would produce thin sequence when sampled at a frequency of

$$f_s = 10\text{Hz}. \quad 7$$

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B.Tech.7<sup>th</sup> Semester Special Examination,2016

Digital Signal Processing

Time : 3 hours

Full Marks : 70

Instructions :

(i) There are **Nine** questions in this paper.

(ii) Attempt **Five** questions in all.

(iii) **Questions No.1 is Compulsory.**

(iv) The marks are indicated in the right hand margin.

1. Answer any seven questions: 2×7=14

(a) Find convolution of  $x[n] = a^n u[n]$  and  $G[n] = u[n]$

(b)  $x[n] = (6-n)u[n] - u[n-6]$

value of sketch of  $y[n] = x[4-n]$

(c) Find the correlation between the sequence

$x(n) = u[n] - u[n-6]$  and  $G[n] = u(n-2) - u(n-5)$

(d) Define the linear phase filter

(e)

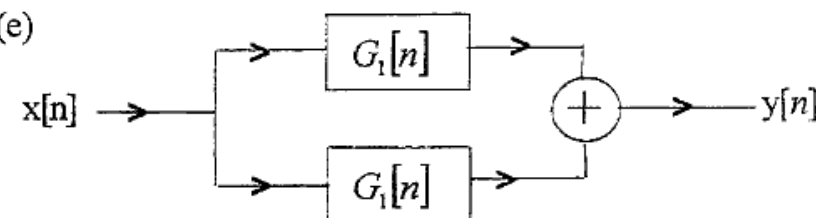


Fig--1

Find the frequency response of the parallel network shown in Fig-1. The systems are Linear shift-invariant systems.

- (f) Find the DTFT of the sequence

$$x_1[n] = \alpha^n u[n] \text{ for } |\alpha| < 1$$

- (g) Let  $G[n]$  be the unit sample response of an linear shift invariant system.

Find the frequency response

$$\text{when } G[n] = \delta[n] + 6\delta[n-1] + 3\delta[n-2]$$

- (h) Explain Nyquist Sampling theorem with proper mathematical expressions

- (i) If  $X(z)$  is  $z$  transform of  $x[n]$ ,

Then find the  $z$  transform of  $nx[n]$

- (j) Let  $x[n]$  be the sequence

$$x[n] = 2\delta[n] + \delta[n-1] + \delta[n-3]$$

then find four-point DFT of  $x[n]$

2. (a) Suppose that a sequence  $x[n]$  has a  $z$  transform. 7

$$X(z) = \frac{4 - \frac{7}{4}z^{-1} + \frac{1}{4}z^{-2}}{1 - \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2}} \text{ with Roc } |z| > \frac{1}{2}$$

find  $x[n]$  using partial fraction expansion method.

- (b) Discuss the advantages of DSP over analog processing. 7

3. (a) The  $z$ -transform of a sequence  $x[n]$  is

$$X(z) = \frac{z + 2z^{-2} + z^{-3}}{1 - 3z^{-4} + z^{-5}} \quad 7$$

if ROC include the unit circle.

Then find the DTFT of  $x[n]$  at  $\omega = \pi$

- (b) Evaluate the convolution of the two sequence 7

$$G[n] = (0.5)^n u[n] \text{ and } x[n] = 3^n u[-n]$$

4. (a) A causal linear shift-invariant system is characterized by the difference equation

$$y[n] = \frac{1}{4}y[n-1] + \frac{1}{8}y[n-2] + x[n] - x[n-1]$$

Find the system function  $H(z)$ , and the unit sample response  $G[n]$ . 7

- (b) How may we compute the N-point DFT of two real-valued sequencer  $x_1(n)$  and  $x_2(n)$ , using one N-point DFT? 7

5. (a) Consider two Sequence 7

$$x_1(n) = \cos\left(\frac{2\pi n}{n}\right) \text{ and } x_2(n) = \sin\left(\frac{2\pi n}{N}\right)$$

Find the N point circular convolution of  $x_1(n)$  with  $x_2(n)$ .

(one DFT property)

- (b) Design a Low pass buffer worth filler to meet the specifications  $f_p = 6kHz$ ,  $f_s = 10kHz$ ,  $S_p = \delta s = 0.1$ . 7

6. Discuss with mathematical expression on decimation in time FFT algorithm also draw the eight point radix-2 butterfly signal flow diagram 14

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P.T.O.